

C2, 1YGB, PAPER M

- 1 -

1. a) BY INSPECTION OR LONG DIVISION

$$\begin{array}{r} x-1 \overline{) 6x^3 - 7x^2 - x + 2} \\ \underline{-6x^3 + 6x^2} \\ -x^2 - x + 2 \\ \underline{x^2 - x} \\ -2x + 2 \\ \underline{2x - 2} \\ 0 \end{array}$$

$$\begin{aligned} \therefore a &= 6 \\ b &= -1 \\ c &= -2 \end{aligned} //$$

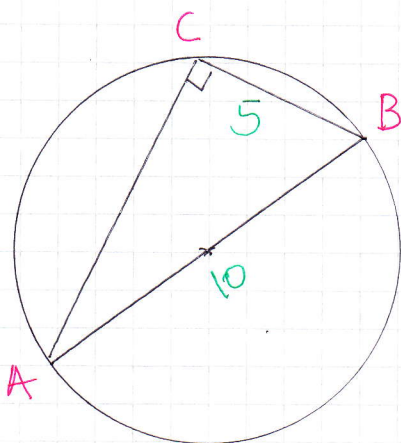
$$\begin{aligned} \text{b) } 6x^3 - 7x^2 - x + 2 &= 0 \\ (x-1)(6x^2 - x - 2) &= 0 \\ (x-1)(3x-2)(2x+1) &= 0 \end{aligned}$$

$$\therefore x = \begin{cases} 1 \\ -\frac{1}{2} \\ \frac{2}{3} \end{cases} //$$

$$\begin{aligned} \text{2. a) b) } x^2 + y^2 - 8x + 6y &= 0 \\ x^2 - 8x + y^2 + 6y &= 0 \\ (x-4)^2 - 16 + (y+3)^2 - 9 &= 0 \\ (x-4)^2 + (y+3)^2 &= 25 \end{aligned}$$

$$\begin{aligned} \therefore \text{CENTRE AT } (4, -3) \\ \text{RADIUS IS } 5 \end{aligned} //$$

9



• EVIDENTLY $|AB|$ IS A DIAMETER
SINCE $|AB| = 10 = 2 \times 5$

• BY PYTHAGORAS

$$|BC|^2 + |CA|^2 = |AB|^2$$

$$5^2 + |CA|^2 = 10^2$$

$$25 + |AC|^2 = 100$$

$$|AC|^2 = 75$$

$$|AC| = \sqrt{75} = 5\sqrt{3} //$$

C2, 1YGB, PAPER M

- 2 -

3. $\frac{\sin x - \cos x}{\cos x} = 2$
 $\Rightarrow \sin x - \cos x = 2\cos x$
 $\Rightarrow \sin x = 3\cos x$
 $\Rightarrow \frac{\sin x}{\cos x} = \frac{3\cos x}{\cos x}$

$\Rightarrow \tan x = 3$

$\arctan(3) = 71.57$

$x = 71.57 \pm 180n$

$n = 0, 1, 2, 3, \dots$

$x_1 = 71.57^\circ$

$x_2 = 251.57^\circ$

4. $y = x^3 - 6x^2 + 12x - 5$

$\frac{dy}{dx} = 3x^2 - 12x + 12$

SOULT FOR ZERO

$\Rightarrow 3x^2 - 12x + 12 = 0$

$\Rightarrow x^2 - 4x + 4 = 0$

$\Rightarrow (x-2)^2 = 0$

$\Rightarrow x = 2$

$\therefore y = 2^3 - 6 \times 2^2 + 12 \times 2 - 5$

$y = 8 - 24 + 24 - 5$

$y = 3$

$\therefore (2, 3)$

$\frac{d^2y}{dx^2} = 6x - 12$

$\left. \frac{d^2y}{dx^2} \right|_{x=2} = 0$

POSSIBLE POINT OF INFLEXION

$\left. \frac{d^3y}{dx^3} \right| = 6$

$\left. \frac{d^3y}{dx^3} \right|_{x=2} = 6 \neq 0$

$\therefore (2, 3)$ IS A STATIONARY POINT OF INFLEXION

5. USING THE MEASUREMENTS PROVIDED

$AREA \approx \frac{THICKNESS}{2} [FIRST + LAST + 2 \times REST]$

$\approx \frac{3}{2} [3.85 + 0 + 2(5.20 + 5.50 + 5.20 + 3.85 + 3)]$

≈ 74

$$\begin{aligned}
 6. a) \quad & 5^{2x-1} = 4^{300} \\
 & \Rightarrow \log 5^{2x-1} = \log 4^{300} \\
 & \Rightarrow (2x-1) \log 5 = 300 \log 4 \\
 & \Rightarrow 2x-1 = \frac{300 \log 4}{\log 5} \\
 & \Rightarrow 2x-1 = 258.4059... \\
 & \Rightarrow x \approx 129.70 \\
 & \Rightarrow x \approx 130 \quad \text{/// (3 st)}
 \end{aligned}$$

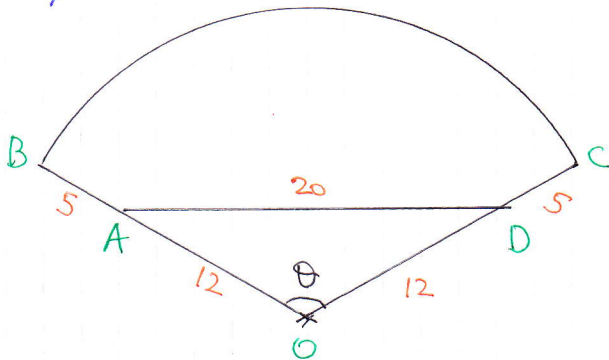
$$\begin{aligned}
 b) \quad & 2^{y+1} = \frac{10}{2^y} \\
 & 2^{y+1} \times 2^y = 10 \\
 & 2^{2y+1} = 10 \\
 & \log 2^{2y+1} = \log 10 \\
 & (2y+1) \log 2 = 1 \\
 & 2y+1 = \frac{1}{\log 2} \\
 & 2y+1 = 3.32... \\
 & y \approx 1.16 \quad \text{/// 3 st.}
 \end{aligned}$$

ALTERNATIVE FOR (b)

$$\begin{aligned}
 & 2^{y+1} = \frac{10}{2^y} \\
 \Rightarrow & \log(2^{y+1}) = \log\left(\frac{10}{2^y}\right) \\
 \Rightarrow & (y+1) \log 2 = \log 10 - \log 2^y \\
 \Rightarrow & (y+1) \log 2 = 1 - y \log 2 \\
 \Rightarrow & (y+1) \log 2 + y \log 2 = 1 \\
 \Rightarrow & (2y+1) \log 2 = 1 \\
 \Rightarrow & 2y+1 = \frac{1}{\log 2}
 \end{aligned}$$

ETC AS BEFORE

7. a)



• BY THE COSINE RULE ON $\triangle AOD$

$$20^2 = 12^2 + 12^2 - 2 \times 12 \times 12 \cos \theta$$

$$400 = 144 + 144 - 288 \cos \theta$$

$$288 \cos \theta = -112$$

$$\cos \theta = -\frac{7}{18}$$

$$\theta \approx 1.97022 \dots$$

$$\theta \approx 1.97^\circ$$

b) AREA OF SECTOR = $\frac{1}{2} r^2 \theta$

$$= \frac{1}{2} \times 17^2 \times 1.97$$

$$\approx 284.697 \dots$$

AREA OF TRIANGLE = $\frac{1}{2} \times 12 \times 12 \times \sin 1.46^\circ$

$$\approx 66.332 \dots$$

(CAN ALSO BE FOUND BY SPLITTING THE TRIANGLE INTO 2 RIGHT ANGLE TRIANGLES

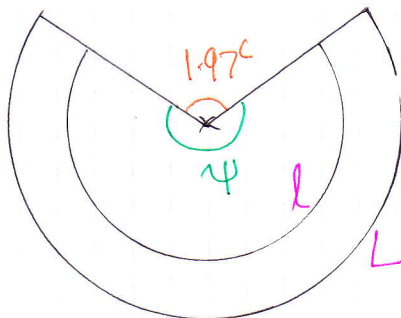
$\sin \phi = \frac{10}{12}$

$$\phi \approx 0.9851 \dots$$

$\theta = 2\phi = 1.97^\circ$)

\therefore AREA OF THE STAFF IS $284.697 - 66.332 \approx 218 \text{ m}^2$ (OR 219 m^2)

c) $\psi = 2\pi - 1.97 \approx 4.31$



$r = 12$
 $R = 15.3$

• $l = r\psi = 12 \times 4.31 = 51.72$

$51.72 \div 0.82 \approx 63$ SEATS

• $L = R\psi = 15.3 \times 4.31 = 65.943 \dots$

$65.943 \div 0.82 \approx 80$ SEATS

\therefore AN EXTRA 17 SEATS

Q2, NYGB, PAPER M

- 5 -

8.

$$a + ar + ar^2 = 33500$$

$$a(1+r+r^2) = 33500$$

$$2000(1+r+r^2) = 33500$$

$$1+r+r^2 = \frac{67}{4}$$

$$4+4r+4r^2 = 67$$

$$4r^2+4r-63=0$$

$$(2r-7)(2r+9)=0$$

$$r = \left\langle \begin{array}{l} \frac{7}{2} \\ \cancel{\frac{-9}{2}} \end{array} \right.$$

Thus LARGEST SHARE IS ar^2

$$2000 \times \left(\frac{7}{2}\right)^2 = 24500$$

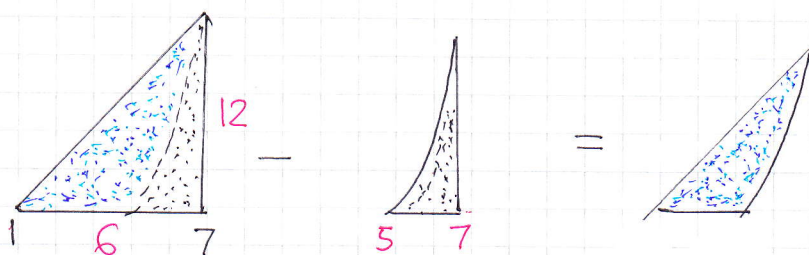
$$4 \neq 24500$$

9.

$$y = x^2 - 6x + 5$$

$$0 = (x-5)(x-1)$$

$$x = \left\langle \begin{array}{l} 5 \\ 1 \end{array} \right. \therefore \begin{array}{l} (5,0) \\ (1,0) \end{array}$$



$$\frac{1}{2} \times 6 \times 12 = 36$$

$$\begin{aligned} \int_5^7 x^2 - 6x + 5 \, dx &= \left[\frac{1}{3}x^3 - 3x^2 + 5x \right]_5^7 \\ &= \left(\frac{343}{3} - 147 + 35 \right) - \left(\frac{125}{3} - 75 + 25 \right) \\ &= \frac{7}{3} - \left(-\frac{25}{3} \right) = \frac{32}{3} \end{aligned}$$

$$\therefore \text{REQUIRED AREA} = 36 - \frac{32}{3} = \frac{76}{3}$$

$$\begin{aligned}
 10. \quad (1+ax)^n &= 1 + \frac{n}{1}(ax)^1 + \frac{n(n-1)}{1 \times 2}(ax)^2 + \frac{n(n-1)(n-2)}{1 \times 2 \times 3}(ax)^3 + \dots \\
 &= 1 + \boxed{na}x + \boxed{\frac{1}{2}n(n-1)a^2}x^2 + \boxed{\frac{1}{6}n(n-1)(n-2)a^3}x^3 + \dots
 \end{aligned}$$

$\begin{matrix} \uparrow & & \uparrow & & \uparrow \\ -30 & & 405 & & b \end{matrix}$

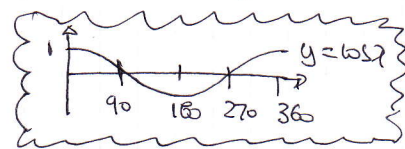
$$\left. \begin{aligned} na &= -30 \\ \frac{1}{2}n(n-1)a^2 &= 405 \end{aligned} \right\} \Rightarrow \left. \begin{aligned} a &= -\frac{30}{n} \\ n(n-1)a^2 &= 810 \end{aligned} \right\} \Rightarrow$$

$$\begin{aligned}
 \Rightarrow n(n-1)\left(-\frac{30}{n}\right)^2 &= 810 \\
 \Rightarrow \cancel{n}(n-1) \times \frac{900}{\cancel{n}^2} &= 810 \\
 \Rightarrow \frac{900(n-1)}{n} &= 810 \\
 \Rightarrow 900n - 900 &= 810n \\
 \Rightarrow 90n &= 900 \\
 n &= 10
 \end{aligned}$$

$$\begin{aligned}
 a &= -\frac{30}{10} \\
 a &= -3 \\
 b &= \frac{1}{6}n(n-1)(n-2)a^3 \\
 b &= \frac{1}{6} \times 10 \times 9 \times 8 \times (-3)^3 \\
 b &= -3240
 \end{aligned}$$

11. a) $A = 5$ (SINCE MINIMUM HAS y VALUE -5)

$B = 40$ SINCE $(90, 0)$ OF $y = \cos x$
 NOW APPEARS AS $(139, 0)$
 (OR THE $180^\circ \rightarrow 220^\circ$)



b) $C = 5$ MUST HAVE THE SAME AMPLITUDE (HEIGHT)

$D = 50$ $(180, 0)$ OF $y = \sin x$ NOW
 APPEARS AS $(139, 0)$

